

AD-A155 231 MODELS FOR MULTIDIMENSIONAL TESTS AND HIERARCHICALLY  
STRUCTURED TRAINING. (U) AMERICAN COLL TESTING PROGRAM  
IOWA CITY IA TEST DEVELOPMENT D. M D RECKASE MAY 85  
UNCLASSIFIED RR-85-1-ONR N00014-81-K-0817 F/G 14/2

MODELS FOR MULTIDIMENSIONAL TESTS AND HIERARCHICALLY  
STRUCTURED TRAINING. (U) AMERICAN COLL TESTING PROGRAM  
IOWA CITY IA TEST DEVELOPMENT D. M D RECKASE MAY 85  
RR-85-1-ONR N00014-81-K-0817 F/G 14/2

**1/1**

UNCLASSIFIED

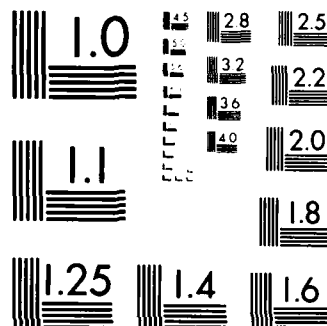
RR-85-1-QNR N00014-81-K-0817

F/G 14/2

NL

END

## RESULTS



MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS 1963-A

AD-A155 231

②  
M

## Final Report

# Models for Multidimensional Tests and Hierarchically Structured Training Materials

Mark D. Reckase

Research Report ONR85-1  
May 1985

**ACT**

The American College Testing Program  
Assessment Programs Area  
Test Development Division  
Iowa City, Iowa 52243

DTIC  
ELECTE  
JUN 18 1985  
S  
B

DTIC FILE COPY

Prepared under Contract No. N00014-81-K0817  
with the Personnel and Training Research Programs  
Psychological Sciences Division  
Office of Naval Research

Approved for public release; distribution unlimited.  
Reproduction in whole or in part is permitted for  
any purpose of the United States Government.

## REPORT DOCUMENTATION PAGE

1a REPORT SECURITY CLASSIFICATION <b>UNCLASSIFIED</b>			1b RESTRICTIVE MARKINGS		
2a SECURITY CLASSIFICATION AUTHORITY			3 DISTRIBUTION / AVAILABILITY OF REPORT Approved for public release: distribution unlimited. Reproduction in whole or in part is permitted for any purpose of the United States Government		
2b DECLASSIFICATION / DOWNGRADING SCHEDULE					
4 PERFORMING ORGANIZATION REPORT NUMBER(S)  ONR 85-1			5 MONITORING ORGANIZATION REPORT NUMBER(S)		
6a NAME OF PERFORMING ORGANIZATION  ACT		6b OFFICE SYMBOL (If applicable)	7a NAME OF MONITORING ORGANIZATION PERSONNEL & TRAINING RESEARCH PROGRAMS OFFICE OF NAVAL RESEARCH		
6c ADDRESS (City, State, and ZIP Code)  P.O. Box 168 Iowa City, IA 52243			7b ADDRESS (City, State, and ZIP Code)  Arlington, VA 22217		
8a NAME OF FUNDING / SPONSORING ORGANIZATION		8b OFFICE SYMBOL (If applicable)	9 PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER  N00014-81-K0817		
8c ADDRESS (City, State, and ZIP Code)			10 SOURCE OF FUNDING NUMBERS		
			PROGRAM ELEMENT NO 61153N	PROJECT NO RR042-04	TASK NO 042-04-01
11 TITLE (Include Security Classification)  Models for multidimensional tests and hierarchically structured training materials.					
12 PERSONAL AUTHOR(S) Mark D. Reckase					
13a TYPE OF REPORT Final Report		13b TIME COVERED FROM 81SEP01 TO 85FEB28		14. DATE OF REPORT (Year, Month, Day) 1985, May	
15. PAGE COUNT 20					
16 SUPPLEMENTARY NOTATION					
17 COSATI CODES			18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)  Item response theory    Learning hierarchies Latent trait theory    Multidimensional models		
FIELD	GROUP	SUB-GROUP			
19 ABSTRACT (Continue on reverse if necessary and identify by block number)  Work on item response theory was extended to include two areas that had not been extensively researched previously. They include models for test items that require more than one ability for a correct response and models for the interaction between modules of instruction that have a hierarchical relationship. For both of these types of models, estimation procedures were developed for model parameters and extensive work was done to determine the appropriate interpretation of the parameter values. This report is a summary of work performed on these models over a three year period.					
20 DISTRIBUTION / AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input checked="" type="checkbox"/> SAME AS RPT <input type="checkbox"/> DTIC USERS			21 ABSTRACT SECURITY CLASSIFICATION		
22a NAME OF RESPONSIBLE INDIVIDUAL Dr. Charles Davis			22b TELEPHONE (Include Area Code) (202) 696-4046		22c OFFICE SYMBOL

# Contents

	Page
Introduction.....	1
Development and Evaluation of MIRT Models.....	2
Analysis of the General Rasch Model.....	6
Interpretation of the Model Parameters.....	11
Summary and Conclusions.....	13
Models for Performance on Hierarchically Structured	
Training Materials.....	14
The Module Characteristic Curve Model.....	16
Summary and Conclusions.....	18
References.....	20

Accession For	
Microfilm	<input checked="" type="checkbox"/>
Microfiche	<input type="checkbox"/>
Microform	<input type="checkbox"/>
Other	
By	
Institution/	
Availability Codes	
Local and/or	
Dist	Special
A-1	



Final Report  
Models for Multidimensional Tests  
and Hierarchically Structural Training Materials

Since the 1950's, there has been increasing interest in psychological and educational measurement that is based upon probabilistic models of the interaction between a person and a test item. These model-based procedures demonstrate how strong assumptions can be used to gain increased control over the measurement process. For example, using item response theory (IRT), the precision of measurement at every point along an ability scale can be determined. Also, items can be selected from a pool to form a test with any desired level of precision at any point on the score scale.

The strong assumptions needed for these model-based procedures are basically that the probabilistic model that has been selected accurately reflects the test data, and that local independence holds for the model. This latter assumption means that the response to one item does not affect the response to another item, and that the response by one person does not affect the response by another person.

Most of the current models assume that the measuring instrument measures only a single trait (Rasch, 1960; Lord, 1952; Birnbaum, 1968). For many tests, this assumption is at least approximated, and for other tests, it is unlikely to be met at all. Most of the current models also are limited to describing a person's response to a single item. In some cases this limitation may make it difficult to solve some measurement problems.

The purpose of the research done on this contract was to extend the types of models available for model-based measurement. Two types of extensions were considered. The first was an extension of item response theory models to the

case where the measurement device was not assumed to be measuring a single dimension. These models were labelled multidimensional item response theory (MIRT) models.

The second type of extension was to cases where sets of related items were considered as a unit. These related sets of items were assumed to be measuring educational constructs that could be arranged into a hierarchy that facilitated learning. These models could be used to determine the interrelationship between the constructs in the hierarchy and the level that must be reached on each construct before a person should be moved on to the next higher level of the hierarchy. Models for tests used with hierarchically arranged instructional units were labelled models for hierarchically structured tests (HST).

The approach taken to develop and evaluate the MIRT and HST models was to first logically evaluate the characteristics of potential models, then to develop estimation procedures for the parameter of the models, and finally to evaluate the models on their ability to describe real test data. These steps were performed separately for a wide class of models of each type. The results of the research will now be described for each type of model, with the analysis of the MIRT models being presented first. Only a summary of the outcome of the research will be presented here, but references will be made to papers and technical reports that contain the details of the research efforts.

#### The Development and Evaluation of MIRT Models

The class of possible multidimensional, probabilistic models of the interaction between a person and a test item is essentially infinite in

size. Any expression that maps a vector of abilities into a probability could be considered as a MIRT model.

Therefore, the first step in the research effort was to limit the possible models to a manageable subset. This was done by reviewing the literature to determine what MIRT models had been proposed. The review identified three general classes of models that had been suggested for use with multidimensional data.

The first of the classes of models considered were extensions of the general model proposed by Rasch (1961). This model, in its most general form, is given by

$$P(x_{ij} | \theta_j, \sigma_i) = \frac{1}{\gamma(\theta_j, \sigma_i)} e^{[\phi(x_{ij})' \theta_j + \psi(x_{ij})' \sigma_i + \theta_j' \chi(x_{ij}) \sigma_i + \rho(x_{ij})]} \quad (1)$$

where  $P(x_{ij} | \theta_j, \sigma_i)$  is the probability of response  $x_{ij}$  given the values of vector parameters  $\theta_j$  and  $\sigma_i$ ;  $\theta_j$  is a vector of parameters that describes the characteristics of person  $j$ ;  $\sigma_i$  is a vector of parameters that describes item  $i$ ;  $\gamma(\theta_j, \sigma_i)$  is a normalizing function defined by

$$\gamma(\theta_j, \sigma_i) = \sum_{x_{ij}} e^{[\phi(x_{ij})' \theta_j + \psi(x_{ij})' \sigma_i + \theta_j' \chi(x_{ij}) \sigma_i + \rho(x_{ij})]} \quad (2)$$

that ensures that the sum of the probabilities of the responses to this item is equal to 1.0;  $\phi(x_{ij})$  is a vector of scoring weights that indicates the value to be given to each response to the items when considering the estimation of the ability parameters;  $\psi(x_{ij})$  is a vector of scoring weights that indicates the value to be given to each response to the item when considering the estimation of item parameters;  $\chi(x_{ij})$  is a matrix of scoring weights that indicates the value to be given to different products of the

elements of  $\delta_j$  and  $\sigma_i$ ; and  $\rho(x_{ij})$  is a constant that is used to set the origin of the linear function defined by the exponent. This equation defines a very general class of models that specifies the dimensionality of the complete latent space by a linear function in the exponent of the logistic model form. Note that this model allows one ability to compensate for another in the metric of  $\theta_j$ . That is, a high value of  $\theta_{j1}$  can compensate for a low value of  $\theta_{jn}$  in the linear function of  $\theta_j$  defined by

$$\psi_1(x_{ij})^{\theta_{j1}} + \psi_2(x_{ij})^{\theta_{j2}} + \dots + \psi_m(x_{ij})^{\theta_{jm}} \quad (3)$$

The same type of linear compensation is present for the item parameters.

The second class of models considered was proposed by Mulaik (1972).

This class of models is of the form

$$P(x_{ij} | \theta_j, \sigma_i) = \frac{\sum_{k=1}^m e^{(\theta_{jk} + \sigma_{ik})x_{ij}}}{1 + \sum_{k=1}^m e^{(\theta_{jk} + \sigma_{ik})}} \quad (4)$$

where  $x_{ij} = 0,1$ ;  $m$  is the number of dimensions; and all of the other terms have been defined previously. This model specifies the dimensionality of the complete latent space as a sum of exponential terms. Ability and item parameters can also compensate for each other in this model, but the compensation occurs on an exponential scale. An interesting point to note is that if each exponent is zero in this model, the probability of a correct response is  $m/(m+1)$ . Thus, as the number of dimensions,  $m$ , increases, the

probability of a correct response increases unless all of the person and item parameters are rescaled. For the model presented in Equation 1, the probability is always .5 when the exponent is zero.

The third class of models that was considered was proposed by Simpson (1978) and in a slightly different form by Whitely (1980). This class of models is of the general form given by

$$P(x_{ij}=1 | \theta_j, \mathbf{a}_i, \mathbf{b}_i, c_i) = c_i + (1-c_i) \prod_{k=1}^m \frac{e^{a_{ik}(\theta_{jk} - b_{ik})}}{1 + e^{a_{ik}(\theta_{jk} - b_{ik})}} \quad (5)$$

where  $\mathbf{a}_i$  is a vector of discrimination parameters,  $\mathbf{b}_i$  is a vector of difficulty parameters,  $c_i$  is the lower asymptote of the probability function, and all of the other terms have been defined previously. This class of models determines the probability of a response based on abilities in a multidimensional space as the product of a series of probability like terms. These terms are, in effect, the probability of the response to the item if the item only required the one dimension. The overall probability is the product of the probabilities on each dimension. If the exponent is zero on each dimension, the probability will be  $c_i + (1 - c_i) (.5)^m$ . Thus, the probability of a correct response will be reduced as each additional dimension is included, unless the parameters are rescaled for each level of dimensionality.

Since the models given in Equations 4 and 5 both require a rescaling of the ability scales with each change in dimensionality, and because both of these models present some very difficult problems in parameter estimation, they were removed from initial consideration and the model presented in Equation 1 became the focus of research effort.

### Analysis of the General Rasch Model

The model presented in Equation 1 defines a very rich class of special cases. By selectively setting the weight functions to zero, many different possible models can be derived, each of which have different properties. Each of these special cases was studied both through a mathematical analysis of the equation for each model and through a statistical analysis of simulated data generated using each model. The results of these analyses were reported in a technical report and in a series of papers presented at professional meetings. The full references to the report and the papers are given below.

McKinley, R. L. and Reckase, M. D. (1982). The use of the general Rasch model with multidimensional item response data (Research Report ONR 82-1). Iowa City, IA: The American College Testing Program.

McKinley, R. L. and Reckase, M. D. (1982, March). Multidimensional latent trait models. Paper presented at the meeting of the National Council on Measurement in Education, New York.

McKinley, R. L. and Reckase, M. D. (1982, May). An analysis of the characteristics of a family of IRT models. Paper presented at the meeting of the Psychometric Society, Montreal.

The results of these analyses showed that two special cases of the general Rasch were capable of modeling realistic multidimensional item response data. The first case uses only the  $\theta_j' x(x_{1j})\sigma_1$  and  $\psi(x_{1j})'\sigma_1$  terms

of the general model. The weights for the other terms were set to zero. The model for this case is given by

$$P(x_{ij} | \theta_j, \sigma_i) = \frac{1}{\gamma(\theta_j, \sigma_i)} e^{(\sum_{k=1}^m \sigma_{ik} \theta_{jk} + \sum_{k=1}^m \sigma_{i,m+k})} \quad (6)$$

where the symbols have been defined earlier. This form of the model can be written in the more familiar form given by

$$P(x_{ij} | \theta_j, a_i, d_i) = \frac{e^{(\sum_{k=1}^m a_{ik} \theta_{jk} + d_i)}}{1 + e^{(\sum_{k=1}^m a_{ik} \theta_{jk} + d_i)}} \quad (7)$$

where  $a_{ik} = \sigma_{ik}$ ,  $d_i = -\sum_{k=1}^m a_{ik} b_{ik} = \sum_{k=1}^m \sigma_{i, m+k}$ ,  $1 + e^{(\sum_{k=1}^m a_{ik} \theta_{jk} + d_i)} = \gamma(\theta_j, \sigma_i)$  and  $a_{ik}$  and  $b_{ik}$  can be interpreted as the  $a$ - and  $b$ -parameters from unidimensional IRT models. Equation 7 can also be thought of as a multidimensional extension of the two-parameter logistic model; therefore, it has been labelled the M2PL model.

The second special case of the general Rasch model that was found to model multidimensional item response data uses only the  $\phi(x_{ij})' \theta_j$  and  $\psi(x_{ij})' \sigma_i$  terms from the general model. This model is of the form

$$P(x_{ij} | \theta_j, \sigma_i) = \frac{1}{\gamma(\theta_j, \sigma_i)} e^{(\phi(x_{ij})' \theta_j + \psi(x_{ij})' \sigma_i)} \quad (8)$$

where all of the terms have been defined previously. This model has been labelled the "cluster model" because in order for it to model multidimensional data,  $x_{ij}$  must be the response string for a cluster of items rather than the response to a single item. If the item cluster contains two dichotomously scored items, the possible  $x_{ij}$  responses would be 0,0; 0,1; 1,0; and 1,1. For each of these responses, a different weight function would be available for the  $\theta$ - and  $\sigma$ -vectors.

Although the cluster model was very promising, it had one difficulty that made it less attractive. In order to use the model, items had to be clustered, and no rigorous means for doing the clustering has been developed. Therefore, research efforts concentrated on the M2PL model.

#### Estimation of Model Parameters

In order for a model to be useful, it must be possible to estimate the parameters of the model. Once the M2PL model was selected as the model for further research efforts, work was begun on developing procedures for estimating the model parameters. Two different approaches were taken to solve the estimation problem: (a) unconditional maximum likelihood, and (b) conditional maximum likelihood. Once computer programs were developed for these two approaches, they were validated using both simulated test data generated from the M2PL model, and real test data that were selected because of their multivariate properties. The estimation procedures and the results of the program validation studies were presented in the publications and papers listed below.

McKinley, R. L. and Reckase, M. D. (1983). MAXLOG: a computer program for the estimation of the parameters of a multidimensional logistic model. Behavior Research Methods and Instrumentation, 15(3), 389-390.

McKinley, R. L. and Reckase, M. D. (1983). An application of a multidimensional extension of the two-parameter logistic latent trait model (Research Report ONR83-3). Iowa City, IA: The American College Testing Program.

Reckase, M. D. and McKinley, R. L. (1982, July). Some latent trait theory in a multidimensional latent space. Paper presented at the Invitational Conference on IRT/CAT, Wayzata, MN.

Reckase, M. D. and McKinley, R. L. (1982, August). The feasibility of a multidimensional latent trait model. Paper presented at the meeting of the American Psychological Association, Washington, D.C.

McKinley, R. L. (1983, April). A multidimensional extension of the two-parameter logistic latent trait model. Paper presented at the meeting of the National Council on Measurement in Education, Montreal.

McKinley, R. L. and Reckase, M. D. (1983, April). The use of IRT analysis on dichotomous data from multidimensional tests. Paper presented at the meeting of the American Educational Research Association, Montreal.

19 April 1985

Defense Technical  
Information Center  
Cameron Station, Bldg 5  
Alexandria, VA 22304  
Attn: TC  
(12 Copies)

Dr. Stephen Dunbar  
Lindquist Center  
for Measurement  
University of Iowa  
Iowa City, IA 52242

Dr. Kent Eaton  
Army Research Institute  
5001 Eisenhower Blvd.  
Alexandria, VA 22333

Dr. John M. Eddins  
University of Illinois  
352 Engineering Research  
Laboratory  
103 South Mathews Street  
Urbana, IL 61801

Dr. Susan Embertson  
University of Kansas  
Psychology Department  
Lawrence, KS 66045

ERIC Facility-Acquisitions  
4833 Rugby Avenue  
Bethesda, MD 20014

Dr. Benjamin A. Fairbank  
Performance Metrics, Inc.  
5825 Callaghan  
Suite 225  
San Antonio, TX 78228

Dr. Pat Federico  
Code P13  
NPRDC  
San Diego, CA 92152

Dr. Leonard Feldt  
Lindquist Center  
for Measurement  
University of Iowa  
Iowa City, IA 52242

Dr. Richard L. Ferguson  
American College Testing  
Program  
P.O. Box 168  
Iowa City, IA 52240

Dr. Gerhard Fischer  
Liebiggasse 5/3  
A 1010 Vienna  
AUSTRIA

Dr. Myron Fischl  
Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Prof. Donald Fitzgerald  
University of New England  
Department of Psychology  
Armidale, New South Wales 2351  
AUSTRALIA

Mr. Paul Foley  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Bob Frey  
Commandant (G-P-1/2)  
USCG HQ  
Washington, DC 20593

Dr. Janice Gifford  
University of Massachusetts  
School of Education  
Amherst, MA 01002

Dr. Robert Glaser  
Learning Research  
& Development Center  
University of Pittsburgh  
3939 O'Hara Street  
Pittsburgh, PA 15260

Dr. Bert Green  
Johns Hopkins University  
Department of Psychology  
Charles & 34th Street  
Baltimore, MD 21218

H. William Greenup  
Education Advisor (E031)  
Education Center, MCDEC  
Quantico, VA 22134

19 April 1985

Dr. James Carlson  
American College Testing  
Program  
P.O. Box 168  
Iowa City, IA 52243

Dr. John B. Carroll  
409 Elliott Rd.  
Chapel Hill, NC 27514

Dr. Robert Carroll  
NAVOP 01B7  
Washington, DC 20370

Mr. Raymond E. Christal  
AFHRL/MOE  
Brooks AFB, TX 78235

Dr. Norman Cliff  
Department of Psychology  
Univ. of So. California  
University Park  
Los Angeles, CA 90007

Director  
Manpower Support and  
Readiness Program  
Center for Naval Analysis  
2000 North Beauregard Street  
Alexandria, VA 22311

Scientific Advisor  
to the DCNO (MPT)  
Center for Naval Analysis  
2000 North Beauregard Street  
Alexandria, VA 22311

Chief of Naval Education  
and Training  
Liason Office  
AFHRL  
Operations Training Division  
Williams AFB, AZ 85224

Assistant Chief of Staff  
Research, Development,  
Test, and Evaluation  
Naval Education and  
Training Command (N-5)  
NAS Pensacola, FL 32508

Office of the Chief  
of Naval Operations  
Research Development  
& Studies Branch  
NAVOP 01B7  
Washington, DC 20350

Dr. Stanley Collyer  
Office of Naval Technology  
800 N. Quincy Street  
Arlington, VA 22217

Dr. Hans Crombag  
University of Leyden  
Education Research Center  
Boerhaavelaan 2  
2334 EN Leyden  
The NETHERLANDS

CTB/McGraw-Hill Library  
2500 Garden Road  
Monterey, CA 93940

CDR Mike Curran  
Office of Naval Research  
800 N. Quincy St.  
Code 270  
Arlington, VA 22217-5000

Mr. Timothy Davey  
University of Illinois  
Educational Psychology  
Urbana, IL 61801

Dr. Dattprasad Divgi  
Syracuse University  
Department of Psychology  
Syracuse, NY 13210

Dr. Hei-Ki Dong  
Ball Foundation  
800 Roosevelt Road  
Building C, Suite 206  
Glen Ellyn, IL 60137

Dr. Fritz Drasgow  
University of Illinois  
Department of Psychology  
603 E. Daniel St.  
Champaign, IL 61820

Distribution List

Personnel Analysis Division  
AF/MPXA  
5C360, The Pentagon  
Washington, DC 20330

Air Force Human Resources Lab  
AFHRL/MPD  
Brooks AFB, TX 78235

Air Force Office  
of Scientific Research  
Life Sciences Directorate  
Bolling Air Force Base  
Washington, DC 20332

Dr. Robert Ahlers  
Code N711  
Human Factors Laboratory  
NAVTRAEQUIPCEN  
Orlando, FL 32813

Dr. Erling B. Andersen  
Department of Statistics  
Stuadiestraede 6  
1455 Copenhagen  
DENMARK

Technical Director  
Army Research Institute for the  
Behavioral and Social Sciences  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Special Assistant for Projects  
OASN(M&RA)  
5D800, The Pentagon  
Washington, DC 20350

Dr. Alan Baddeley  
Medical Research Council  
Applied Psychology Unit  
15 Chaucer Road  
Cambridge CB2 2EF  
ENGLAND

Dr. Patricia Baggett  
University of Colorado  
Department of Psychology  
Boulder, CO 80309

Dr. Isaac Bejar  
Educational Testing Service  
Princeton, NJ 08450

CDR Robert J. Biersner, USN  
Naval Biodynamics Laboratory  
P. O. Box 29407  
New Orleans, LA 70189

Dr. Menucha Birenbaum  
School of Education  
Tel Aviv University  
Tel Aviv, Ramat Aviv 69978  
Israel

Dr. Werner Birke  
Personalstammamt  
der Bundeswehr  
D-5000 Koeln 90  
WEST GERMANY

Code N711  
Attn: Arthur S. Blaiwes  
Naval Training Equipment Center  
Orlando, FL 32813

Dr. R. Darrell Bock  
University of Chicago  
Department of Education  
Chicago, IL 60637

Dr. Nick Bond  
Office of Naval Research  
Liaison Office, Far East  
APO San Francisco, CA 96503

Dr. Robert Breaux  
Code N-095R  
NAVTRAEQUIPCEN  
Orlando, FL 32813

Dr. Robert Brennan  
American College Testing  
Programs  
P. O. Box 168  
Iowa City, IA 52243

Dr. Patricia A. Butler  
NIE Mail Stop 1806  
1200 19th St., NW  
Washington, DC 20208

References

- Birnbaum, A. (1968). Some latent trait models and their use in inferring an examinee's ability. In F.M. Lord and M.R. Novick, Statistical theories of mental test scores. Reading, MA: Addison-Wesley.
- Lord, F.M. (1952). A theory of test scores. Psychometric Monograph, 7.
- Mulaik, S.A. (1972, March). A mathematical investigation of some multidimensional Rasch models for psychological tests. Paper presented at the meeting of the Psychometric Society, Princeton, NJ.
- Rasch, G. (1960). Probabilistic models for some intelligence and attainment tests. Copenhagen: Danish Institute for Educational Research.
- Rasch, G. (1962). On general laws and the meaning of measurement in psychology. Proceedings of the Fourth Berkely Symposium on Mathematical Statistics and Probability, 4, 321-334.
- Sympson, J.B. (1978). A model for testing with multidimensional items. In D.J. Weiss (Ed.), Proceedings for the 1977 Computerized Adaptive Testing Conference. Minneapolis: University of Minnesota.
- Whitely, S.E. (1980). Measuring aptitude processes with multicomponent latent trait models (Technical Report No. NIE-80-5). Lawrence, KS: University of Kansas, Department of Psychology.

real test data that should be hierarchically related. However, the upper and lower asymptotes did not appear to be needed for the particular real data set that was analyzed. Further studies need to be done to determine whether this is a general finding applicable to all hierarchically arranged modules, or whether it only applies to this case. If the  $c$ - and  $e$ -parameters are not needed, the model can be simplified to a two-parameter logistic model.

One problem with the use of the model became evident with the analysis of the real test data. In order to accurately estimate the parameters of the model, examinees must be routed to the higher level unit of instruction even when they have not performed well on the lower level unit. This is poor educational practice and, in many cases, this data collection procedure cannot be followed. This makes it difficult to obtain data for use in estimating the parameters of the model. It may be that the model will have to be modified to accommodate the routing procedures that are currently being used in modularized instructional programs.

k scale specified by the b-parameter is the suggested decision point on module k for routing to module j if misclassification errors in either direction are considered equally serious.

In order to evaluate this model, it was applied to both simulated and real test data to determine whether the estimation procedures worked properly, and whether it realistically represented actual test results. The outcome of these studies were presented in the following documents.

McKinley, R. L. and Reckase, M. D. (1984). A latent trait model for sequentially arranged units of instruction. Iowa City, IA: The American College Testing Program.

McKinley, R. L. and Reckase, M. D. (1984, April). A latent trait model for use with sequentially arranged units of instruction. Paper presented at the meeting of the American Educational Research Association, New Orleans.

The studies showed that the parameters of the model could be accurately estimated and that for one set of real test data, the model gave very reasonable results. There was some indications, however, that the upper and lower asymptote parameters might not be needed. It may be possible to simplify the model to a two-parameter logistic form.

#### Summary and Conclusions

A model for the relationship between modules of instruction that are hierarchically related was proposed and evaluated using both simulated and real test data. The results of the studies showed that the model parameters could be accurately estimated and that the model was a good representation of

where  $P_j(\theta_{ik})$  is the probability of passing module  $j$  given level of performance  $\theta_{ik}$  of examinee  $i$  on prerequisite module  $k$ ,  $c_j$  is the probability of passing module  $j$  if the examinee has not acquired any knowledge in module  $k$ ,  $e_j$  is the probability of passing module  $j$  if the examinee has mastered module  $k$ ,  $D = 1.7$ ,  $a_j$  is a parameter related to the strength of the relationship between the two modules, and  $b_j$  is the difficulty of the passing score used on module  $j$ . This model predicts the probability that an examinee will pass module  $j$  based on his/her performance on module  $k$ .

In order to use this model, estimates of achievement are first obtained on module  $k$ . This can either be done by analyzing the module  $k$  test using an IRT model, or by converting the raw scores on module  $k$  to  $z$ -scores. These achievement measures are then used as known values and the model parameters are estimated using a maximum likelihood estimation procedure.

A very low  $a$ -parameter estimate is an indication that the two modules are not very highly related. A high  $a$ -value indicates that knowledge on module  $k$  is very important for module  $j$ . A high estimate for the  $c$ -parameter indicates that examinees can perform well on module  $j$  even without mastering module  $k$ . A low  $c$ -value indicates that an examinee cannot perform well on module  $j$  unless knowledge has been acquired on module  $k$ .

Estimates of the  $e$ -parameter indicate the maximum probability of passing the  $j$  module given that the examinee has mastered module  $k$ . Low values indicate that module  $k$  contains only a small portion of the information needed to pass module  $j$ . High values indicate that module  $k$  includes most of the information needed to pass module  $j$ .

The  $b$ -parameter estimates indicate the point on the module  $k$  scale that best distinguishes between persons who pass or fail module  $j$ . This point will change with changes in the passing score on module  $j$ . The point on the module

coefficients of dependence were found to provide insufficient information for validating the sequence of instructional units, or for setting passing scores. The procedures based on mathematical models were found to have great potential, but the currently available procedures did not seem to meet the needs of instructional programs. There seemed to be a clear need for a procedure that could be used to arrange units of instruction into a hierarchy based upon the prerequisite knowledge required by each unit of instruction, and that could be used to set passing scores for each unit that would improve the efficiency and accuracy of the routing process. The model proposed and evaluated during this research effort was designed to perform these functions.

#### The Module Characteristic Curve Model

The basic idea behind the proposed model for the interrelationship between modules of instruction is that if two modules form a learning hierarchy, performance on the higher level instructional module is dependent upon prerequisite knowledge obtained from the lower level module of instruction. Thus, if sufficient knowledge has not been gained on the lower level module, a high level of performance cannot be exhibited on the higher level module of instruction. This implies that success on the higher module is related to the level of performance on the lower module.

The probabilistic model that was hypothesized to describe the relationship between hierarchically related instructional modules is given by

$$P_j(\theta_{ik}) = c_j + (1 - c_j - e_j) \frac{e^{Da_j(\theta_{ik} - b_j)}}{1 + e^{Da_j(\theta_{ik} - b_j)}} \quad (9)$$

scores on the tests are used to route the students through the units of instruction. The purpose of this component of the project was to evaluate an IRT-type model that had potential for assisting in determining the interrelationships between the instructional units and in determining the decision points that should be used with each unit test to minimize routing error. The model treats each unit, or module, of instruction as a complex item and hypothesizes a particular mathematical form for the interrelationship between performance on one module and the probability of successfully passing the next module in the instructional program.

The first step in the evaluation of this model for performance in instructional programs was to review the literature in the area called "learning hierarchies" to determine what procedures were currently being used to evaluate the interrelationships between units of instruction and to set passing scores on the unit tests. The information obtained from the review would serve as a basis for comparison for the results obtained from the proposed model. The review of the literature was presented in the following report.

Reckase, M. D. and McKinley, R. L. (1982). The validation of learning hierarchies (Research Report ONR 82-2). Iowa City, IA: The American College Testing Program.

The review of the literature indicated that there were two general types of procedures that had been used to indicate the relationships between instructional units; those based on coefficients of dependence, and those based on a more complete description of the relationships between units of instruction, usually a mathematical model. The procedures based on

multidimensional extension of the two-parameter logistic model was selected as a promising model for future work. Estimation procedures were developed for this model and the results were validated using simulated and real test data. A theoretical foundation was laid for an interpretation of the item parameters of the MIRT models, and definitions of multidimensional item difficulty, discrimination, and information were developed. At this point, a sufficient framework has been developed to make multidimensional item response theory a viable technique.

Although substantial advances have been made in the area of MIRT, even more work is left to be done. The current estimation programs require excessive amounts of computer time when more than two or three dimensions are specified for a model. Work needs to be done to make estimation of the parameter more efficient. Procedures are needed to determine the appropriate number of dimensions for a set of test data, and procedures for indicating the fit of the models to the data are needed. A related question is whether the M2PL model is an accurate representation of the interaction between a person and an item. This model implies that one ability can compensate for another. Perhaps a model of this type is not appropriate. These and other questions will be addressed in future work.

#### Models for Performance on

#### Hierarchically Structured Training Materials

Programs of instruction are often composed of many short, homogenous instructional units that have been arranged according to the logical relationships of the content. In many cases, short tests are given to determine each student's level of competence on a unit of instruction, and the

The second point that became evident was that the locus of points of inflection could change with the direction taken relative to the surface in the multidimensional space. This is a direct consequence of the fact that the slope at a point on the IRS is different in different directions. The direction in the space is one way of indicating the composite of abilities that is of interest.

In order to take these two points into account, a definition of multidimensional difficulty was derived that was based upon a vector conceptualization. The multidimensional difficulty of an item was defined as the direction from the origin of the multidimensional space to the point of steepest slope and the distance from the origin to the point of steepest slope. Discrimination of an item was related to the slope in the difficulty direction at the point of the steepest slope. Information was also given a directional interpretation. For a group centered at the origin of the space, an item is most informative in the difficulty direction. The item information can also be determined in any other direction, but the maximum information will be less than in the direction indicated by the multidimensional difficulty.

The definitions of multidimensional difficulty, discrimination, and information are general enough that they apply to any MIRT model that is monotonically increasing in probability with an increase in any ability dimension. The definition also includes the unidimensional definitions as special cases.

#### Summary and Conclusions

This portion of the research project accomplished several important tasks in the development of MIRT. A number of models were analyzed and the

Reckase, M. D. and McKinley, R. L. (1983, April). The definition of difficulty and discrimination for multidimensional item response theory models. Paper presented at the meeting of the American Educational Research Association, Montreal.

Reckase, M. D. and McKinley, R. L. (1983, June). The item difficulty concept generalized to the multidimensional latent space. Paper presented at the meeting of the Psychometric Society, Los Angeles.

Reckase, M. D. and McKinley, R. L. (1984, June). Multidimensional difficulty as a direction and a distance. Paper presented at the meeting of the Psychometric Society, Santa Barbara, CA.

Initial work in this area concentrated on deriving a direct generalization of the interpretations of the difficulty and discrimination parameters and item and test information from the unidimensional item response theory models to the MIRT models. Since the difficulty of an item was defined for the unidimensional models as the point on the ability scale corresponding to the point of inflection of the item characteristic curve, multidimensional difficulty was conceptually thought of as the point of inflection of the multidimensional item response surface (IRS). An analysis of this approach quickly made two important points evident. First, for an IRT there is not a single point of inflection, but rather a locus of points of inflection. Depending upon the MIRT model and the dimensionality being considered, this locus of points of inflection could be a straight line, a curve, a hyperplane, or a hypersurface. The complexity of the locus of points of inflection made its practical application difficult.

The study showed that the dimensionality of both the items and the examinee population was important in interpreting the results of an M2PL analysis. If each item were a relatively pure measure of an ability, the procedure obtained good estimates of the ability parameters, even when they were correlated. But, as the correlation between ability estimates increased, there was some deterioration of the accuracy of the estimates. When each item measured more than one ability, the effect of correlated abilities was more extreme. As the correlation between abilities increased, the M2PL solution tended to collapse to a single dimension. The results seemed to imply the need for procedures for oblique rotations to improve the recovery of the ability dimensions.

#### Interpretation of the Model Parameters

When a MIRT model is used, estimates can be obtained for the ability and the item parameters. The ability parameter estimates can be interpreted in a fairly straightforward manner as the amount of ability a person has on each dimension. The item parameter estimates, however, do not have the same intuitive meaning. Therefore, a major part of this project dealt with determining the MIRT model analogs to the unidimensional IRT item parameters and the measures of quality, such as item and test information. The results of the work in this area were presented in the following documents.

McKinley, R. L. and Reckase, M. D. (1983). An extension of the two-parameter logistic model to the multidimensional latent space (Research Report ONR83-2). Iowa City, IA: The American College Testing Program.

The results of these studies showed that both the unconditional and conditional maximum likelihood procedures could be used to estimate the item and ability parameters of the M2PL model, but that the unconditional maximum likelihood procedure required somewhat less computer time. However, both procedures require fairly extensive computer facilities, and as the number of dimensions in the model increased, the computer time required became prohibitive. It was clear that improved estimation procedures were needed if the M2PL model was to be widely used.

The validation of the estimation procedures yielded uniformly good results when simulated test results were used. However, when real test data were analyzed, the results were inconsistent. Some studies gave readily interpretable results that were in many ways similar to factor analytic results. In other studies anomalies appeared, such as highly negatively correlated ability estimates that suggested that added constraints were needed to control the estimation process.

In order to study the estimation process in more detail, the M2PL procedure was used to analyze simulated test data that had been produced using a multivariate ability distribution that had varying degrees of correlation between the abilities. The results of the study were presented in the following report.

McKinley, R. L. and Reckase, M. D. (1984). An investigation of the effect of correlated abilities on observed test characteristics (Research Report ONR 84-1). Iowa City, IA: The American College Testing Program.

19 April 1985

Dipl. Pad. Michael W. Habon  
Universität Dusseldorf  
Erziehungswissenschaftliches  
Universitätsstr. 1  
D-4000 Dusseldorf 1  
WEST GERMANY

Dr. Ron Hambleton  
School of Education  
University of Massachusetts  
Amherst, MA 01002

Prof. Lutz F. Hornke  
Universität Dusseldorf  
Erziehungswissenschaftliches  
Universitätsstr. 1  
Dusseldorf 1  
WEST GERMANY

Dr. Paul Horst  
677 G Street, #184  
Chula Vista, CA 90010

Mr. Dick Hoshaw  
NAVOP-135  
Arlington Annex  
Room 2834  
Washington, DC 20350

Dr. Lloyd Humphreys  
University of Illinois  
Department of Psychology  
603 East Daniel Street  
Champaign, IL 61820

Dr. Steven Hunka  
Department of Education  
University of Alberta  
Edmonton, Alberta  
CANADA

Dr. Earl Hunt  
Department of Psychology  
University of Washington  
Seattle, WA 98105

Dr. Huynh Huynh  
College of Education  
Univ. of South Carolina  
Columbia, SC 29208

Dr. Douglas H. Jones  
Advanced Statistical  
Technologies Corporation  
10 Trafalgar Court  
Lawrenceville, NJ 08148

Prof. John A. Keats  
Department of Psychology  
University of Newcastle  
N.S.W. 2308  
AUSTRALIA

Dr. Norman J. Kerr  
Chief of Naval Education  
and Training  
Code 00A2  
Naval Air Station  
Pensacola, FL 32508

Dr. William Koch  
University of Texas-Austin  
Measurement and Evaluation  
Center  
Austin, TX 78703

Dr. Leonard Kroeker  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Patrick Kyllonen  
AFHRL/MOE  
Brooks AFB, TX 78235

Dr. Anita Lancaster  
Accession Policy  
OASD/MI&L/MP&FM/AP  
Pentagon  
Washington, DC 20301

Dr. Daryll Lang  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Jerry Lehnus  
OASD (M&RA)  
Washington, DC 20301

Dr. Thomas Leonard  
University of Wisconsin  
Department of Statistics  
1210 West Dayton Street  
Madison, WI 53705

Dr. Alan M. Lesgold  
Learning R&D Center  
University of Pittsburgh  
Pittsburgh, PA 15260

Dr. Michael Levine  
Educational Psychology  
210 Education Bldg.  
University of Illinois  
Champaign, IL 61801

Dr. Charles Lewis  
Faculteit Sociale Wetenschappen  
Rijksuniversiteit Groningen  
Oude Boteringestraat 23  
9712GC Groningen  
The NETHERLANDS

Dr. Robert Linn  
College of Education  
University of Illinois  
Urbana, IL 61801

Dr. Robert Lockman  
Center for Naval Analysis  
200 North Beauregard St.  
Alexandria, VA 22311

Dr. Frederic M. Lord  
Educational Testing Service  
Princeton, NJ 08541

Dr. James Lumsden  
Department of Psychology  
University of Western Australia  
Nedlands W.A. 6009  
AUSTRALIA

Dr. William L. Maloy (02)  
Chief of Naval Education  
and Training  
Naval Air Station  
Pensacola, FL 32508

Dr. Gary Marco  
Stop 31-E  
Educational Testing Service  
Princeton, NJ 08451

Dr. Glenn Martin  
Army Research Institute  
5001 Eisenhower Blvd.  
Alexandria, VA 22333

Dr. Scott Maxwell  
Department of Psychology  
University of Notre Dame  
Notre Dame, IN 46556

Dr. Samuel T. Mayo  
Loyola University of Chicago  
820 North Michigan Avenue  
Chicago, IL 60611

Dr. James McBride  
Psychological Corporation  
c/o Harcourt, Brace,  
Javanovich Inc.  
1250 West 6th Street  
San Diego, CA 92101

Dr. Clarence McCormick  
HQ, MEPCOM  
MEPCT-P  
2500 Green Bay Road  
North Chicago, IL 60064

Dr. Barbara Means  
Human Resources  
Research Organization  
1100 South Washington  
Alexandria, VA 22314

Dr. Robert Mislevy  
Educational Testing Service  
Princeton, NJ 08541

Dr William Montague  
NPRDC Code 13  
San Diego, CA 92152

Ms. Kathleen Moreno  
Navy Personnel R&D Center  
Code 62  
San Diego, CA 92152

Headquarters, Marine Corps  
Code MPI-20  
Washington, DC 20380

Director  
Research & Analysis Division  
Navy Recruiting Command (Code 22)  
4015 Wilson Plvd.  
Arlington, VA 22203

19 April 1985

Program Manager for Manpower,  
Personnel, and Training  
NAVMAT 0722  
Arlington, VA 22217-5000

Dr. W. Alan Nicewander  
University of Oklahoma  
Department of Psychology  
Oklahoma City, OK 73069

Dr. William E. Nordbrock  
FMC-ADCO Box 25  
APO, NY 09710

Dr. Melvin R. Novick  
356 Lindquist Center  
for Measurement  
University of Iowa  
Iowa City, IA 52242

Director, Manpower and Personnel  
Laboratory  
NPRDC (Code 06)  
San Diego, CA 92152

Library  
Code P201L  
Navy Personnel R&D Center  
San Diego, CA 92152

Technical Director  
Navy Personnel R&D Center  
San Diego, CA 92152

Commanding Officer  
Naval Research Laboratory  
Code 2627  
Washington, DC 20390

Dr. Harry F. O'Neil, Jr.  
Training Research Lab  
Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Dr. James Olson  
WICAT, Inc.  
1875 South State Street  
Orem, UT 84057

Mathematics Group  
Office of Naval Research  
Code 744MA  
800 North Quincy Street  
Arlington, VA 22217-5000

Office of Naval Research  
Code 442PT  
800 N. Quincy Street  
Arlington, VA 22217-5000  
(5 Copies)

Special Assistant for Marine  
Corps Matters  
Code 100M  
Office of Naval Research  
800 N. Quincy St.  
Arlington, VA 22217-5000

Commanding Officer  
Army Research Institute  
ATTN: PERI-BR (Dr. J. Orasanu)  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Dr. Jesse Orlansky  
Institute for Defense Analyses  
1801 N. Beauregard St.  
Alexandria, VA 22311

Dr. Randolph Park  
AFHRL/MOAN  
Brooks AFB, TX 78235

Wayne M. Patience  
American Council on Education  
GED Testing Service, Suite 20  
One Dupont Circle, NW  
Washington, DC 20036

Dr. James Paulson  
Department of Psychology  
Portland State University  
P.O. Box 751  
Portland, OR 97207

Dr. Roger Pennell  
Air Force Human Resources  
Laboratory  
Lowry AFB, CO 80230

Administrative Sciences Department  
Naval Postgraduate School  
Monterey, CA 93940

Department of Operations Research  
Naval Postgraduate School  
Monterey, CA 93940

Dr. Mark D. Reckase  
ACT  
P. O. Box 168  
Iowa City, IA 52243

Dr. Malcolm Ree  
AFHRL/MP  
Brooks AFB, TX 78235

Dr. Carl Ross  
CNET-PDCD  
Building 90  
Great Lakes NTC, IL 60088

Mr. Robert Ross  
Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Dr. Lawrence Rudner  
403 Elm Avenue  
Takoma Park, MD 20012

Dr. J. Ryan  
Department of Education  
University of South Carolina  
Columbia, SC 29208

Dr. Fumiko Samejima  
Department of Psychology  
University of Tennessee  
Knoxville, TN 37916

Mr. Drew Sands  
NPRDC Code 62  
San Diego, CA 92152

Dr. Robert Sasmor  
Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Lowell Schoer  
Psychological & Quantitative  
Foundations  
College of Education  
University of Iowa  
Iowa City, IA 52242

Dr. Mary Schratz  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. W. Steve Sellman  
OASD(MRA&L)  
2B269 The Pentagon  
Washington, DC 20301

Dr. Sylvia A. S. Shafto  
National Institute of Education  
1200 19th Street  
Mail Stop 1806  
Washington, DC 20208

Dr. Joyce Shields  
Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333

Dr. Kazuo Shigemasu  
7-9-24 Kugenuma-Kaigan  
Fujusawa 251  
JAPAN

Dr. William Sims  
Center for Naval Analysis  
200 North Beauregard Street  
Alexandria, VA 22311

Dr. H. Wallace Sinaiko  
Manpower Research  
and Advisory Services  
Smithsonian Institution  
801 North Pitt Street  
Alexandria, VA 22314

Dr. Richard Snow  
Liaison Scientist  
Office of Naval Research  
Branch Office, London  
Box 39  
FPO New York, NY 09510

Dr. Richard Sorensen  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Paul Speckman  
University of Missouri  
Department of Statistics  
Columbia, MO 65201

Martha Stocking  
Educational Testing Service  
Princeton, NJ 08541

Dr. Peter Stoloff  
Center for Naval Analysis  
200 North Beauregard Street  
Alexandria, VA 22311

Dr. William Stout  
University of Illinois  
Department of Mathematics  
Urbana, IL 61801

Maj. Bill Strickland  
AF/MPXOA  
4E168 Pentagon  
Washington, DC 20330

Dr. Hariharan Swaminathan  
Laboratory of Psychometric and  
Evaluation Research  
School of Education  
University of Massachusetts  
Amherst, MA 01003

Mr. Brad Sympson  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. John Tangney  
AFOSR/NL  
Bolling AFB, DC 20332

Dr. Kikumi Tatsuoka  
CERL  
252 Engineering Research  
Laboratory  
Urbana, IL 61801

Dr. Maurice Tatsuoka  
220 Education Bldg  
1310 S. Sixth St.  
Champaign, IL 61820

Dr. David Thissen  
Department of Psychology  
University of Kansas  
Lawrence, KS 66044

Mr. Gary Thomasson  
University of Illinois  
Educational Psychology  
Champaign, IL 61820

Dr. Robert Tsutakawa  
Department of Statistics  
University of Missouri  
Columbia, MO 65201

Dr. Ledyard Tucker  
University of Illinois  
Department of Psychology  
603 E. Daniel Street  
Champaign, IL 61820

Dr. Vern W. Urry  
Personnel R&D Center  
Office of Personnel Management  
1900 E. Street, NW  
Washington, DC 20415

Dr. David Vale  
Assessment Systems Corp.  
2233 University Avenue  
Suite 310  
St. Paul, MN 55114

Dr. Frank Vicino  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Howard Wainer  
Division of Psychological Studies  
Educational Testing Service  
Princeton, NJ 08540

Dr. Ming-Mei Wang  
Lindquist Center  
for Measurement  
University of Iowa  
Iowa City, IA 52242

Mr. Thomas A. Warm  
Coast Guard Institute  
P. O. Substation 18  
Oklahoma City, OK 73169

Dr. Brian Waters  
HumRRO  
300 North Washington  
Alexandria, VA 22314

Dr. Edward Wegman  
Office of Naval Research  
Code 411  
800 North Quincy Street  
Arlington, VA 22217-5000

Dr. David J. Weiss  
N660 Elliott Hall  
University of Minnesota  
75 E. River Road  
Minneapolis, MN 55455

Dr. Donald Weitzman  
MITRE  
1820 Dolley Madison Blvd.  
MacLean, VA 22102

Major John Welsh  
AFHRL/MOAN  
Brooks AFB, TX 78223

Dr. Douglas Wetzel  
Code 12  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Rand R. Wilcox  
University of Southern  
California  
Department of Psychology  
Los Angeles, CA 90007

German Military Representative  
ATTN: Wolfgang Wildegrube  
Streitkraefteamt  
D-5300 Bonn 2  
4000 Brandywine Street, NW  
Washington, DC 20016

Dr. Bruce Williams  
Department of Educational  
Psychology  
University of Illinois  
Urbana, IL 61801

Dr. Hilda Wing  
Army Research Institute  
5001 Eisenhower Ave.  
Alexandria, VA 22333

Ms. Marilyn Wingersky  
Educational Testing Service  
Princeton, NJ 08541

Dr. Martin F. Wiskoff  
Navy Personnel R & D Center  
San Diego, CA 92152

Mr. John H. Wolfe  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. George Wong  
Biostatistics Laboratory  
Memorial Sloan-Kettering  
Cancer Center  
1275 York Avenue  
New York, NY 10021

Dr. Wallace Wulfeck, III  
Navy Personnel R&D Center  
San Diego, CA 92152

Dr. Wendy Yen  
CTB/McGraw Hill  
Del Monte Research Park  
Monterey, CA 93940

Major Frank Yohannan, USMC  
Headquarters, Marine Corps  
(Code MPI-20)  
Washington, DC 20380

Dr. Joseph L. Young  
Memory & Cognitive  
Processes  
National Science Foundation  
Washington, DC 20550

**END**

**FILMED**

7-85

**DTIC**